

CHAPTER 3 (Odd)

1. a. 0.5 in. = 500 mils
b. 0.01 in. = 10 mils
c. 0.004 in. = 4 mils
d. 1 in. = 1000 mils
- e. $0.02 \cancel{\text{ft}} \left[\frac{12 \cancel{\text{in.}}}{1 \cancel{\text{ft}}} \right] \left[\frac{10^3 \text{ mils}}{1 \cancel{\text{in.}}} \right] = 240 \text{ mils}$
- f. $0.01 \cancel{\text{cm}} \left[\frac{1 \text{ in.}}{2.54 \cancel{\text{cm}}} \right] = 0.003937 \text{ in.} = 3.937 \text{ mils}$
3. $A_{\text{CM}} = (d_{\text{mils}})^2 \Rightarrow d_{\text{mils}} = \sqrt{A_{\text{CM}}}$
- a. $d = \sqrt{1600 \text{ CM}} = 40 \text{ mils} = 0.04 \text{ in.}$ b. $d = \sqrt{900 \text{ CM}} = 30 \text{ mils} = 0.03 \text{ in.}$
c. $d = \sqrt{40,000 \text{ CM}} = 200 \text{ mils} = 0.2 \text{ in.}$ d. $d = \sqrt{625 \text{ CM}} = 25 \text{ mils} = 0.025 \text{ in.}$
e. $d = \sqrt{7.75 \text{ CM}} = 2.78 \text{ mils} = 0.00278 \text{ in.}$ f. $d = \sqrt{81 \text{ CM}} = 9 \text{ mils} = 0.009 \text{ in.}$
5. $R = \rho \frac{l}{A}$, $\rho = 9.9$, $50 \text{ yd} = 150 \text{ ft}$
 $0.0045 \text{ in.} = 4.5 \text{ mils}$, $A_{\text{CM}} = (4.5 \text{ mils})^2 = 20.25 \text{ CM}$
 $R = \rho \frac{l}{A} = \frac{(9.9)(150 \text{ ft})}{(20.25 \text{ CM})} = 73.33 \Omega$
7. $\frac{1}{32}'' = 0.03125'' = 31.25 \text{ mils}$, $A_{\text{CM}} = (31.25 \text{ mils})^2 = 976.56 \text{ CM}$
 $R = \rho \frac{l}{A} \Rightarrow l = \frac{RA}{\rho} = \frac{(2.2 \Omega)(976.56 \text{ CM})}{600} = 3.581 \text{ ft}$
9. a. $R_{\text{silver}} > R_{\text{copper}} > R_{\text{aluminum}}$
- b. Silver: $R = \rho \frac{l}{A} = \frac{(9.9)(1 \text{ ft})}{1 \text{ CM}} = 9.9 \Omega$ { $A_{\text{CM}} = (1 \text{ mil})^2 = 1 \text{ CM}$
Copper: $R = \rho \frac{l}{A} = \frac{(10.37)(10 \text{ ft})}{100 \text{ CM}} = 1.037 \Omega$ { $A_{\text{CM}} = (10 \text{ mils})^2 = 100 \text{ CM}$
Aluminum: $R = \rho \frac{l}{A} = \frac{(17)(50 \text{ ft})}{2500 \text{ CM}} = 0.34 \Omega$ { $A_{\text{CM}} = (50 \text{ mils})^2 = 2500 \text{ CM}$
11. a. $3'' = 3000 \text{ mils}$, $1/2'' = 0.5 \text{ in.} = 500 \text{ mils}$
 $\text{Area} = (3 \times 10^3 \text{ mils})(5 \times 10^2 \text{ mils}) = 15 \times 10^5 \text{ sq. mils}$
 $15 \times 10^5 \text{ sq mils} \left[\frac{4/\pi \text{ CM}}{1 \text{ sq mil}} \right] = 19.108 \times 10^5 \text{ CM}$
 $R = \rho \frac{l}{A} = \frac{(10.37)(4')}{19.108 \times 10^5 \text{ CM}} = 21.71 \mu\Omega$

$$b. \quad R = \rho \frac{l}{A} = \frac{(17)(4')}{19.108 \times 10^5 \text{ CM}} = 35.59 \mu\Omega$$

c. increases

d. decreases

$$13. \quad A = \frac{\pi d^2}{4} \Rightarrow d = \sqrt{\frac{4A}{\pi}} = \sqrt{\frac{4(0.04 \text{ in.}^2)}{\pi}} = 0.2257 \text{ in.}$$

$$d_{\text{mils}} = 225.7 \text{ mils}$$

$$A_{\text{CM}} = (225.7 \text{ mils})^2 = 50,940.49 \text{ CM}$$

$$\frac{R_1}{R_2} = \frac{\rho_1 \frac{l_1}{A_1}}{\rho_2 \frac{l_2}{A_2}} = \frac{\cancel{\rho_1} l_1 A_2}{\cancel{\rho_2} l_2 A_1} = \frac{l_1 A_2}{l_2 A_1} \quad (\rho_1 = \rho_2)$$

$$\text{and } R_2 = \frac{R_1 l_2 A_1}{l_1 A_2} = \frac{(800 \text{ m}\Omega)(300 \text{ ft})(40,000 \text{ CM})}{(200 \text{ ft})(50,940.49 \text{ CM})} = 942.28 \text{ m}\Omega$$

$$15. \quad a. \quad \#8: R = 1800 \cancel{\text{ft}} \left[\frac{0.6282 \Omega}{1000 \cancel{\text{ft}}} \right] = 1.1308 \Omega$$

$$\#18: R = 1800 \cancel{\text{ft}} \left[\frac{6.385 \Omega}{1000 \cancel{\text{ft}}} \right] = 11.493 \Omega$$

$$b. \quad \#18:\#8 = 11.493 \Omega:1.1308 \Omega = 10.164:1 \cong 10:1$$

$$c. \quad \#18:\#8 = 1624.3 \text{ CM}:16,509 \text{ CM} = 1:10.164 \cong 1:10$$

$$17. \quad a. \quad A/\text{CM} = 230 \text{ A}/211,600 \text{ CM} = 1.087 \text{ mA}/\text{CM}$$

$$b. \quad \frac{1.087 \text{ mA}}{\cancel{\text{CM}}} \left[\frac{1 \cancel{\text{CM}}}{\frac{\pi}{4} \cancel{\text{sq mils}}} \right] \left[\frac{1000 \cancel{\text{mils}}}{1 \text{ in.}} \right] \left[\frac{1000 \cancel{\text{mils}}}{1 \text{ in.}} \right] = 1.384 \text{ kA}/\text{in.}^2$$

$$c. \quad 5 \cancel{\text{kA}} \left[\frac{1 \text{ in.}^2}{1.348 \cancel{\text{kA}}} \right] = 3.6127 \text{ in.}^2$$

$$19. \quad a. \quad \frac{1''}{2} \left[\frac{2.54 \text{ cm}}{1''} \right] = 1.27 \text{ cm}, \quad 3 \cancel{\mu\text{ft}} \left[\frac{2.54 \text{ cm}}{1 \cancel{\mu\text{ft}}} \right] = 7.62 \text{ cm}$$

$$4 \cancel{\text{ft}} \left[\frac{12 \cancel{\mu\text{ft}}}{1 \cancel{\text{ft}}} \right] \left[\frac{2.54 \text{ cm}}{1 \cancel{\mu\text{ft}}} \right] = 121.92 \text{ cm}$$

$$R = \rho \frac{l}{A} = \frac{(1.724 \times 10^{-6})(121.92 \text{ cm})}{(1.27 \text{ cm})(7.62 \text{ cm})} = 21.71 \mu\Omega$$

$$b. \quad R = \rho \frac{l}{A} = \frac{(2.825 \times 10^{-6})(121.92 \text{ cm})}{(1.27 \text{ cm})(7.62 \text{ cm})} = 35.59 \mu\Omega$$

c. increases

d. decreases

$$21. \quad R = R_s \frac{l}{w} \Rightarrow w = \frac{R_s l}{R} = \frac{(150 \, \Omega)(1/2 \, \text{in.})}{500 \, \Omega} = 0.15 \, \text{in.}$$

$$23. \quad \frac{234.5 + t_1}{R_1} = \frac{234.5 + t_2}{R_2} \Rightarrow \frac{234.5 + 10}{2 \, \Omega} = \frac{234.5 + 60}{R_2}$$

$$R_2 = \frac{(294.5)(2 \, \Omega)}{244.5} = 2.409 \, \Omega$$

$$25. \quad C = \frac{5}{9}(\text{°F} - 32) = \frac{5}{9}(32 - 32) = 0^\circ (=32^\circ\text{F})$$

$$C = \frac{5}{9}(70 - 32) = 21.11^\circ (=70^\circ\text{F})$$

$$\frac{234.5^\circ + 21.11^\circ}{4 \, \Omega} = \frac{234.5^\circ + 0^\circ}{R_2}$$

$$R_2 = \frac{(234.5)(4 \, \Omega)}{255.61} = 3.67 \, \Omega$$

$$27. \quad \frac{243 + (-30)}{0.04 \, \Omega} = \frac{243 + 0}{R_2}$$

$$R_2 = \frac{(243)(40 \, \text{m}\Omega)}{213} = 46 \, \text{m}\Omega$$

$$29. \quad \text{a.} \quad \frac{238.5}{0.92 \, \Omega} = \frac{234.5 + t_2}{1.06 \, \Omega}$$

$$274.793 = 234.5 + t_2$$

$$t_2 = 40.29^\circ\text{C}$$

$$\text{b.} \quad \frac{238.5}{0.92 \, \Omega} = \frac{234.5 + t_2}{0.15 \, \Omega}$$

$$38.886 = 234.5 + t_2$$

$$t_2 = -195.61^\circ\text{C}$$

$$31. \quad \text{a.} \quad \alpha_{20} = \frac{1}{|T| + 20^\circ\text{C}} = \frac{1}{234.5 + 20} = \frac{1}{254.5} = 0.003929 \approx 0.00393$$

$$\text{b.} \quad R = R_{20}[1 + \alpha_{20}(t - 20^\circ\text{C})]$$

$$1 \, \Omega = 0.8 \, \Omega[1 + 0.00393(t - 20^\circ)]$$

$$1.25 = 1 + 0.00393t - 0.0786$$

$$1.25 - 0.9214 = 0.00393t$$

$$0.3286 = 0.00393t$$

$$t = \frac{0.3286}{0.00393} = 83.61^\circ\text{C}$$

$$33. \quad \text{Table: } 1000' \text{ of \#12 copper wire} = 1.588 \, \Omega @ 20^\circ\text{C}$$

$$C^\circ = \frac{5}{9}(F^\circ - 32) = \frac{5}{9}(115 - 32) = 46.11^\circ\text{C}$$

$$R = R_{20}[1 + \alpha_{20}(t - 20^\circ\text{C})]$$

$$= 1.588 \, \Omega[1 + 0.00393(46.11 - 20)]$$

$$= 1.751 \, \Omega$$

35. Fig. 3.21: At 90°C , $+1\% = 0.01(10,000) = 100\ \Omega$, $\therefore 10,100\ \Omega$ at 90°C

$$\Delta R = R_2 - R_1 = 10,100\ \Omega - 10,000 = 100\ \Omega$$

$$\Delta T = 90^\circ - 20^\circ\text{C} = 70^\circ\text{C}$$

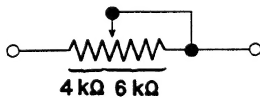
$$\text{PPM} = \frac{(\Delta R)(10^6)}{(R_{\text{nominal}})(\Delta T)} = \frac{(100\ \Omega)(10^6)}{(10\ \text{k}\Omega)(70)} = 142.86$$

41. $-30^\circ\text{C} \Rightarrow +2\% = 200\ \Omega \Rightarrow 10.2\ \text{k}\Omega$

$$100^\circ\text{C} \Rightarrow 1.5\% = 150\ \Omega \Rightarrow 10.15\ \text{k}\Omega$$

43. $6.5\ \text{k}\Omega$

- 45.



47. a. $220\ \Omega = \text{Red, Red, Brown, Silver}$

- b. $4700\ \Omega = \text{Yellow, Violet, Red, Silver}$

- c. $68\ \text{k}\Omega = \text{Blue, Gray, Orange, Silver}$

- d. $9.1\ \text{M}\Omega = \text{White, Brown, Green, Silver}$

49. $10\ \Omega \pm 10\% = 10\ \Omega \pm 1\ \Omega = 9\ \Omega - 11\ \Omega$
 $15\ \Omega \pm 10\% = 15\ \Omega \pm 1.5\ \Omega = 13.5\ \Omega - 16.5\ \Omega$ } No

51. a. Table 3.2, $\Omega/1000' = 6.385\ \Omega$

$$G = \frac{1}{R} = \frac{1}{6.385\ \Omega} = 156.6\ \text{mS}$$

$$\text{or } G = \frac{A}{\rho l} = \frac{1,624.3\ \text{CM (Table 3.2)}}{(10.37)(1000')} = 156.6\ \text{mS}$$

- b. $G = \frac{1,624.3\ \text{CM}}{(17)(1000')} = 95.54\ \text{mS (Al)}$

- c. $G = \frac{1,624.3\ \text{CM}}{(74)(1000')} = 21.95\ \text{mS (Fe)}$

53. Good: $R < 1\ \Omega$ (low)

$$\text{Bad: } R = \infty\ \Omega$$

55. Good: Some resistance (filament not open)

$$\text{Bad: } R = \infty\ \Omega \text{ (filament open)}$$

57. a. Log scale: $10\ \text{fc} \Rightarrow 3\ \text{k}\Omega$

$$100\ \text{fc} \Rightarrow 0.4\ \text{k}\Omega$$

- b. negative

- c. no—log scales imply linearity

- d. $1\ \text{k}\Omega \Rightarrow \cong 30\ \text{fc}$

$$10\ \text{k}\Omega \Rightarrow \cong 2\ \text{fc}$$

$$\left| \frac{\Delta R}{\Delta \text{fc}} \right| = \frac{10\ \text{k}\Omega - 1\ \text{k}\Omega}{30\ \text{fc} - 2\ \text{fc}} = 321.43\ \Omega/\text{fc}$$

$$\text{and } \frac{\Delta R}{\Delta \text{fc}} = -321.43\ \Omega/\text{fc}$$

CHAPTER 3 (Even)

2. a. $0.050 \text{ in.} = 50 \text{ mils}, A_{\text{CM}} = (50 \text{ mils})^2 = 2500 \text{ CM}$
 b. $0.016 \text{ in.} = 16 \text{ mils}, A_{\text{CM}} = (16 \text{ mils})^2 = 256 \text{ CM}$
 c. $0.30 \text{ in.} = 300 \text{ mils}, A_{\text{CM}} = (300 \text{ mils})^2 = 90 \times 10^3 \text{ CM}$
 d. $[0.1 \cancel{\text{cm}}] \left[\frac{1 \text{ in.}}{2.54 \cancel{\text{cm}}} \right] = 0.0394 \text{ in.} = 39.4 \text{ mils}$
 $A_{\text{CM}} = (39.4 \text{ mils})^2 = 1552.36 \text{ CM}$
 e. $0.003 \cancel{\text{ft}} \left[\frac{12 \text{ in.}}{1 \cancel{\text{ft}}} \right] = 0.036 \text{ in.} = 36 \text{ mils}$
 $A_{\text{CM}} = (36 \text{ mils})^2 = 1296 \text{ CM}$
 f. $0.0042 \cancel{\text{m}} \left[\frac{39.37 \text{ in.}}{1 \cancel{\text{m}}} \right] = 0.1654 \text{ in.} = 165.4 \text{ mils}$
 $A_{\text{CM}} = (165.4 \text{ mils})^2 = 27,357.16 \text{ CM}$
4. $0.01 \text{ in.} = 10 \text{ mils}, A_{\text{CM}} = (10 \text{ mils})^2 = 100 \text{ CM}$
 $R = \rho \frac{l}{A} = (10.37) \frac{(200')}{100 \text{ CM}} = 20.74 \Omega$
6. a. $A = \rho \frac{l}{R} = \frac{(17)(80')}{2.5 \Omega} = 544 \text{ CM}$
 b. $d = \sqrt{A_{\text{CM}}} = \sqrt{544 \text{ CM}} = 23.32 \text{ mils} = 0.0233 \text{ in.}$
8. a. $A_{\text{CM}} = \rho \frac{l}{R} = \frac{(10.37)(300')}{2.5 \Omega} = 1244.40 \text{ CM}$ b. larger c. smaller
10. $\rho = \frac{RA}{l} = \frac{(500 \Omega)(94 \text{ CM})}{1000'} = 47 \Rightarrow \text{nickel}$
12. $l_2 = 2l_1, A_2 = A_1/4, \rho_2 = \rho_1$

$$\frac{R_2}{R_1} = \frac{\frac{\rho_2 l_2}{A_2}}{\frac{\rho_1 l_1}{A_1}} = \frac{\rho_2 l_2 A_1}{\rho_1 l_1 A_2} = \frac{2l_1 A_1}{l_1 A_1/4} = 8$$

 and $R_2 = 8R_1 = 8(0.2 \Omega) = 1.6 \Omega$
 $\Delta R = 1.6 \Omega - 0.2 \Omega = 1.4 \Omega$
14. a. #11: $450 \cancel{\text{ft}} \left[\frac{1.260 \Omega}{1000 \cancel{\text{ft}}} \right] = 0.567 \Omega$
 #14: $450 \cancel{\text{ft}} \left[\frac{2.525 \Omega}{1000 \cancel{\text{ft}}} \right] = 1.136 \Omega$

b. Resistance: #14:#11 = $1.136 \Omega:0.567 \Omega \cong 2:1$

c. Area: #14:#11 = $4106.8 \text{ CM}:8234.0 \text{ CM} \cong 1:2$

16. a. $A = \rho \frac{l}{R} = \frac{(10.37)(30')}{6 \text{ m}\Omega} = \frac{311.1 \text{ CM}}{6 \times 10^{-3}} = 51,850 \text{ CM} \Rightarrow \#3$
but 110 A $\Rightarrow \#2$

b. $A = \rho \frac{l}{R} = \frac{(10.37)(30')}{3 \text{ m}\Omega} = \frac{311.1 \text{ CM}}{3 \times 10^{-3}} = 103,700 \text{ CM} \Rightarrow \#0$

18. $\frac{1}{10} \text{ in.} = 0.1 \text{ in.} \left[\frac{2.54 \text{ cm}}{1 \text{ in.}} \right] = 0.254 \text{ cm}$
 $A = \frac{\pi d^2}{4} = \frac{(3.14)(0.254 \text{ cm})^2}{4} = 0.0506 \text{ cm}^2$
 $l = \frac{RA}{\rho} = \frac{(2 \Omega)(0.0506 \text{ cm}^2)}{1.724 \times 10^{-6}} = 58,700 \text{ cm} = 58.7 \text{ m}$

20. $R_s = \frac{\rho}{d} = 100 \Rightarrow d = \frac{\rho}{100} = \frac{250 \times 10^{-6}}{100} = 2.5 \mu\text{cm}$

22. a. $d = 1 \text{ in.} = 1000 \text{ mils}$
 $A_{\text{CM}} = (10^3 \text{ mils})^2 = 10^6 \text{ CM}$
 $\rho_1 = \frac{RA}{l} = \frac{(1 \text{ m}\Omega)(10^6 \text{ CM})}{10^3 \text{ ft}} = 1 \text{ CM-}\Omega/\text{ft}$

b. $1 \text{ in.} = 2.54 \text{ cm}$
 $A = \frac{\pi d^2}{4} = \frac{\pi(2.54 \text{ cm})^2}{4} = 5.067 \text{ cm}^2$
 $l = 1000 \text{ ft} \left[\frac{12 \text{ in.}}{1 \text{ ft}} \right] \left[\frac{2.54 \text{ cm}}{1 \text{ in.}} \right] = 30,480 \text{ cm}$
 $\rho_2 = \frac{RA}{l} = \frac{(1 \text{ m}\Omega)(5.067 \text{ cm}^2)}{30,480 \text{ cm}} = 1.662 \times 10^{-7} \Omega\text{-cm}$

c. $k = \frac{\rho_2}{\rho_1} = \frac{1.662 \times 10^{-7} \Omega\text{-cm}}{1 \text{ CM-}\Omega/\text{ft}} = 1.662 \times 10^{-7}$

24. $\frac{236 + 0}{0.02 \Omega} = \frac{236 + 100}{R_2}$
 $R_2 = \frac{(0.02 \Omega)(336)}{236} = 0.028 \Omega$

26. $\frac{234.5 + 30}{0.76 \Omega} = \frac{234.5 - 40}{R_2}$
 $R_2 = \frac{(194.5)(0.76 \Omega)}{264.5} = 0.5589 \Omega$

$$\frac{234.5 + 20}{0.002} = \frac{234.5 + 0}{R_2}$$

$$212^{\circ}\text{F} = 100^{\circ}\text{C}$$

$$R_2 = \frac{(334.5)(2 \text{ m}\Omega)}{254.5} = 2.628 \text{ m}\Omega$$

$$^{\circ}\text{C} = -234.5^{\circ}$$

Absolute zero ($R = 0 \Omega$)

$\therefore 10 \text{ k}\Omega$

44. **6.25 k Ω and 18.75 k Ω**

46. a. $56,000 \pm 5\% = 56,000 \Omega \pm 2800 \Omega = 53,200 \Omega - 58,800 \Omega$

b. $220 \Omega \pm 10\% = 220 \Omega \pm 22 \Omega = 198 \Omega - 242 \Omega$

c. $10 \Omega \pm 20\% = 10 \Omega \pm 2 \Omega = 8 \Omega - 12 \Omega$

48. $\left. \begin{array}{l} 10 \Omega \pm 20\% \Rightarrow 8 \Omega \rightarrow 12 \Omega \\ 15 \Omega \pm 20\% \Rightarrow 12 \Omega \rightarrow 18 \Omega \end{array} \right\} \text{Yes}$

50. a. $G = \frac{1}{0.086 \Omega} = 11.628 \text{ S}$ b. $G = \frac{1}{4000 \Omega} = 0.25 \text{ mS}$

c. $G = \frac{1}{2.2 \times 10^6 \Omega} = 0.4545 \mu\text{S}$

$G_a > G_b > G_c$ vs $R_c > R_b > R_a$

52. $A_2 = 1\frac{2}{3} A_1 = \frac{5}{3} A_1, l_2 = \left[1 - \frac{2}{3}\right] l_1 = \frac{l_1}{3}, \rho_2 = \rho_1$

$$\frac{G_1}{G_2} = \frac{\frac{\rho_1 \frac{A_1}{l_1}}{\frac{\rho_2 \frac{A_2}{l_2}}}}{\frac{\rho_2 \frac{A_2}{l_2}}{\frac{\rho_1 \frac{A_1}{l_1}}}}} = \frac{\frac{\rho_1 \frac{A_1}{l_1}}{\frac{\rho_2 \frac{A_2}{l_2}}}}{\frac{\rho_2 \frac{A_2}{l_2}}{\frac{\rho_1 \frac{A_1}{l_1}}}}} = \frac{\left[\frac{l_1}{3}\right] A_1}{l_1 \left[\frac{5}{3} A_1\right]} = \frac{1}{5}$$

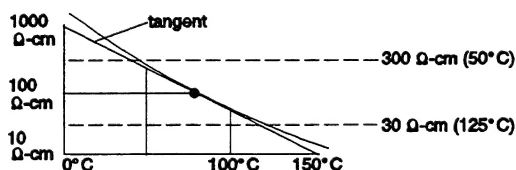
$G_2 = 5G_1 = 5(100 \text{ S}) = 500 \text{ S}$

56. a. -50°C specific resistance $\cong 10^5 \Omega\text{-cm}$
 50°C specific resistance $\cong 300 \Omega\text{-cm}$
 200°C specific resistance $\cong 7 \Omega\text{-cm}$

b. negative

c. No

d. $\rho = \frac{\Delta \Omega\text{-cm}}{\Delta T} = \frac{300 - 30}{125 - 50} = \frac{270 \Omega\text{-cm}}{75^\circ\text{C}} \cong 3.6 \Omega\text{-cm}/^\circ\text{C}$



58. @ 0.5 mA, $V \cong 195 \text{ V}$

@ 1 mA, $V \cong 200 \text{ V}$

@ 5 mA, $V \cong 215 \text{ V}$

$\Delta V_{\text{total}} = 215 \text{ V} - 195 \text{ V} = 20 \text{ V}$

5 mA:0.5 mA = 10:1

compared to

215 V:200 V = 1.075:1